

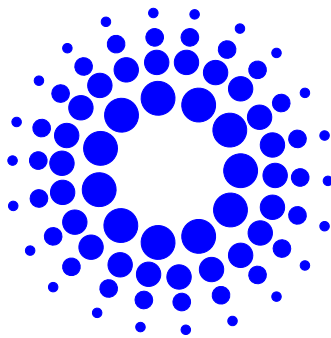
XMM ESA' project

Mandrel #19 assessment
at the E.S.R.F.

Surface roughness, Diffuse scattering, Slope errors

Theory, Measurements, Data processing, Results

Image modeling



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